



Year 12 Syllabus in a nutshell

IB Maths AI SL





Year 12 Syllabus in a nutshell – IB Applications and Interpretations SL

NB The * denotes sections of the course that are covered by both routes i.e. Analysis and Approaches AND Applications and Interpretation

Topic	Guide Reference	Summary
Sequences and Series	SL1.2* SL1.3* SL1.4* SL1.6 (AA only) SL1.8 (AA only) SL1.9 (AA only)	Arithmetic sequences and series , use of the formulae for the n th term and the sum of the first n terms of the sequence, use of sigma notation for sums of arithmetic sequences, Applications of arithmetic sequences, analysis, interpretation and prediction where a model is not perfectly arithmetic in real life. Geometric sequences and series, Use of the formulae for the n th term and the sum of the first n terms of the sequence , Use of sigma notation for sums of geometric sequences, Applications of geometric sequences, Sum of infinite convergent geometric sequences Financial applications of geometric sequences and series: compound interest and annual depreciation Simple deductive proof, numerical and algebraic; how to lay out a left-hand side to right-hand side (LHS to RHS) proof , The symbols and notation for equality and identity The binomial theorem: expansion of $(a + b)^n, n \in \mathbb{N}$
Linear Geometry	SL2.1* SL2.4* SL3.5	Different forms of the equation of a straight line , Gradient; intercepts, Lines with gradients, m_1 and m_2 Parallel lines $m_1 = m_2$, Perpendicular lines $m_1 \times m_2 = -1$ Determine key features of graphs, Finding the point of intersection of two curves or lines using technology Equations of perpendicular bisectors.
Geometry and Trigonometry in 2D and 3D	SL1.6 SL3.1* SL3.2* SL3.3*	Approximation: decimal places, significant figures , Upper and lower bounds of rounded numbers , Percentage errors Estimation The distance between two points in three- dimensional space, and their midpoint , Volume and surface area of three- dimensional solids including right-pyramid, right cone, sphere, hemisphere and combinations of these solids , The size of an angle between two intersecting lines or between a line and a plane Use of sine, cosine and tangent ratios to find the sides and angles of right-angled triangles , The sine rule: $a/\sin A = b/\sin B = c/\sin C$, The cosine rule: $c^2 = a^2 + b^2 - 2ab \sin C$; $\cos C = \frac{a^2 + b^2 - c^2}{2ab}$, Area of a triangle as $\frac{1}{2} ab \sin C$ Applications of right and non-right-angled trigonometry, including Pythagoras' theorem , Angles of elevation and depression , Construction of labelled diagrams from written statements
Statistics	SL4.1* SL4.2* SL4.3* SL4.4*	Concepts of population, sample, random sample, discrete and continuous data , Reliability of data sources and bias in sampling , Interpretation of outliers , Sampling techniques and their effectiveness



		<p>Presentation of data (discrete and continuous): frequency distributions (tables) , Histograms , Cumulative frequency; cumulative frequency graphs; use to find median, quartiles, percentiles, range and interquartile range (IQR) , Production and understanding of box and whisker diagrams.</p> <p>Measures of central tendency (mean, median and mode) , Estimation of mean from grouped data , Modal class , Measures of dispersion (interquartile range, standard deviation and variance) , Effect of constant changes on the original data , Quartiles of discrete data</p> <p>Linear correlation of bivariate data , Pearson’s product–moment correlation coefficient, r , Scatter diagrams; lines of best fit, by eye, passing through the mean point , Equation of the regression line of y on x , Use of the equation of the regression line for prediction purposes , Interpret the meaning of the parameters, a and b, in a linear regression $y = ax + b$</p>
Functions	SL2.2* SL2.3* SL2.4* SL2.5 SL1.8 SL2.6	<p>Modelling with the following functions: Linear models: $f(x) = mx + c$, Quadratic models: $f(x) = ax^2 + bx + c$; $a \neq 0$. , Axis of symmetry, vertex, zeros and roots, intercepts on the x-axis and y-axis , Exponential growth and decay models: $f(x) = ka^x + c$ $f(x) = ka^{-x} + c$ (for $a > 0$) $f(x) = ke^{rx} + c$ Equation of a horizontal asymptote. , Direct/inverse variation: $f(x) = ax^n$, $n \in \mathbb{Z}$ The y-axis as a vertical asymptote when $n < 0$, Cubic models: $f(x) = ax^3 + bx^2 + cx + d$, Sinusoidal models: $f(x) = a \sin(bx) + d$, $f(x) = a \cos(bx) + d$</p> <p>Use technology to solve: Systems of linear equations in up to 3 variables Polynomial equations</p> <p>Modelling skills: Use the modelling process described in the “mathematical modelling” section to create, fit and use the theoretical models in section 2.5, and their graphs , Develop and fit the model: Given a context recognize and choose an appropriate model and possible parameters. , Determine a reasonable domain for a model , Find the parameters of a model. , Test and reflect upon the model: Comment on the appropriateness and reasonableness of a model. , Justify the choice of a particular model, based on the shape of the data, properties of the curve and/or on the context of the situation , Use the model: Reading, interpreting and making predictions based on the model</p>
Basic Differentiation	SL5.1* SL5.2* SL5.3* SL5.4* SL5.6 SL5.7	<p>Introduction to the concept of a limit , Derivative interpreted as gradient function and as rate of change</p> <p>Increasing and decreasing functions , Graphical interpretation of $f'(x) > 0$, $f'(x) = 0$, $f'(x) < 0$</p> <p>Derivative of $f(x) = ax^n$ $f'(x) = anx^{n-1}$, $n \in \mathbb{Z}$, The derivative of functions of the form $f(x) = ax^n - bx^{n-1} \dots$ where all exponents are integers</p> <p>Tangents and normals at a given point, and their equations</p> <p>Values of x where the gradient of a curve is zero , Solution of $f'(x) = 0$, Local maximum and minimum points</p> <p>Optimisation problems in context</p>
Probability	SL4.2* SL4.5* SL4.6* SL4.7* SL4.8* SL4.9*	<p>Presentation of data (discrete and continuous): frequency distributions (tables) , Histograms , Cumulative frequency; cumulative frequency graphs; use to find median, quartiles, percentiles, range and interquartile range (IQR)</p> <p>Production and understanding of box and whisker diagrams.</p>



		<p>Concepts of trial, outcome, equally likely outcomes, relative frequency, sample space (U) and event, The probability of an event A is $P(A) = n(A)/n(U)$, The complementary events A and A' (not A), Expected number of occurrences</p> <p>Use of Venn diagrams, tree diagrams, sample space diagrams and tables of outcomes to calculate probabilities, Combined events: $P(A \cup B) = P(A) + P(B) - P(A \cap B)$, Mutually exclusive events: $P(A \cap B) = 0$ Conditional probability: $P(A/B) = P(A \cap B)/P(B)$ Independent events: $P(A \cap B) = P(A)P(B)$.</p> <p>Formal definition and use of the formulae: $P(A B) = P(A \cap B)/P(B)$ for conditional probabilities, and $P(A B) = P(A) = P(A B')$ for independent events</p> <p>Concept of discrete random variables and their probability distributions, Expected value (mean), for discrete data, Applications</p> <p>Binomial distribution, Mean and variance of the binomial distribution</p> <p>The normal distribution and curve, Properties of the normal distribution, Diagrammatic representation, Normal probability calculations, Inverse normal calculations</p>
Trigonometry	SL2.1* SL2.3* SL2.4* SL3.1* SL3.5 SL3.6	<p>Different forms of the equation of a straight line, Gradient; intercepts, Lines with gradients, m_1 and m_2 Parallel lines $m_1 = m_2$, Perpendicular lines $m_1 \times m_2 = -1$</p> <p>The graph of a function; its equation $y = f(x)$, Creating a sketch from information given or a context, including transferring a graph from screen to paper, Using technology to graph functions including their sums and differences</p> <p>Determine key features of graphs, Finding the point of intersection of two curves or lines using technology</p> <p>The distance between two points in three-dimensional space, and their midpoint, Volume and surface area of three-dimensional solids including right-pyramid, right cone, sphere, hemisphere and combinations of these solids, The size of an angle between two intersecting lines or between a line and a plane</p> <p>Equations of perpendicular bisectors.</p> <p>Voronoi diagrams; sites, vertices, edges, cells, Addition of a site to an existing Voronoi diagram, Nearest neighbour interpolation, Applications of 'the toxic waste dump' problem</p>